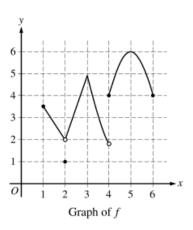
## Spring Break Practice Exam No Calculator Multiple Choice

- 1. If  $y = x \sin x$ , then  $\frac{dy}{dx} =$ 
  - (A)  $\sin x + \cos x$
  - (B)  $\sin x + x \cos x$
  - (C)  $\sin x x \cos x$
  - (D)  $x(\sin x + \cos x)$
  - (E)  $x(\sin x \cos x)$
- 2. Let f be the function given by  $f(x) = 300x x^3$ . On which of the following intervals is the function f increasing?
  - (A)  $\left(-\infty, -10\right]$  and  $\left[10, \infty\right)$
  - (B) [-10, 10]
  - (C) [0, 10] only
  - (D)  $[0, 10\sqrt{3}]$  only
  - (E) [0, ∞)
- 3.  $\int \sec x \tan x \, dx =$ 
  - (A)  $\sec x + C$
  - (B)  $\tan x + C$
  - (C)  $\frac{\sec^2 x}{2} + C$
  - (D)  $\frac{\tan^2 x}{2} + C$
  - (E)  $\frac{\sec^2 x \tan^2 x}{2} + C$
- 4. If  $f(x) = 7x 3 + \ln x$ , then f'(1) =
  - (A) 4
- (B) 5
- (C) 6
- (D) 7
- (E) 8



- 5. The graph of the function f is shown above. Which of the following statements is false?
  - (A)  $\lim_{x\to 2} f(x)$  exists.
  - (B)  $\lim_{x\to 3} f(x)$  exists.
  - (C)  $\lim_{x \to 4} f(x)$  exists.
  - (D)  $\lim_{x \to 5} f(x)$  exists.
  - (E) The function f is continuous at x = 3.
- 6. A particle moves along the x-axis. The velocity of the particle at time t is  $6t t^2$ . What is the total distance traveled by the particle from time t = 0 to t = 3?
  - (A) 3
- (B) 6
- (C) 9
- (D) 18
- (E) 27

7. If 
$$y = (x^3 - \cos x)^5$$
, then  $y' =$ 

$$(A) \ 5\left(x^3 - \cos x\right)^4$$

(B) 
$$5(3x^2 + \sin x)^4$$

(C) 
$$5(3x^2 + \sin x)$$

(D) 
$$5(3x^2 + \sin x)^4 \cdot (6x + \cos x)$$

(E) 
$$5(x^3 - \cos x)^4 \cdot (3x^2 + \sin x)$$

t (hours)	4	7	12	15
R(t) (liters/hour)	6.5	6.2	5.9	5.6

- 8. A tank contains 50 liters of oil at time t = 4 hours. Oil is being pumped into the tank at a rate R(t), where R(t)is measured in liters per hour, and t is measured in hours. Selected values of R(t) are given in the table above. Using a right Riemann sum with three subintervals and data from the table, what is the approximation of the number of liters of oil that are in the tank at time t = 15 hours?
  - (A) 64.9
- (B) 68.2
- (C) 114.9
- (D) 116.6 (E) 118.2

$$f(x) = \begin{cases} \frac{(2x+1)(x-2)}{x-2} & \text{for } x \neq 2\\ k & \text{for } x = 2 \end{cases}$$

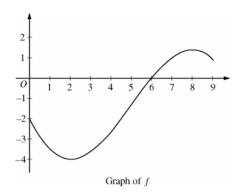
- 9. Let f be the function defined above. For what value of k is f continuous at x = 2?
  - (A) 0
- (B) 1
- (C) 2
- (D) 3
- (E) 5
- 10. What is the area of the region in the first quadrant bounded by the graph of  $y = e^{x/2}$  and the line x = 2?

- (A) 2e-2 (B) 2e (C)  $\frac{e}{2}-1$  (D)  $\frac{e-1}{2}$  (E) e-1
- 11. Let f be the function defined by  $f(x) = \sqrt{|x-2|}$  for all x. Which of the following statements is true?
  - (A) f is continuous but not differentiable at x = 2.
  - (B) f is differentiable at x = 2.
  - (C) f is not continuous at x = 2.
  - (D)  $\lim_{x \to 2} f(x) \neq 0$
  - (E) x = 2 is a vertical asymptote of the graph of f.
- 12. Using the substitution  $u = \sqrt{x}$ ,  $\int_{1}^{4} \frac{e^{\sqrt{x}}}{\sqrt{x}} dx$  is equal to which of the following?
  - (A)  $2\int_{1}^{16} e^{u} du$  (B)  $2\int_{1}^{4} e^{u} du$  (C)  $2\int_{1}^{2} e^{u} du$  (D)  $\frac{1}{2}\int_{1}^{2} e^{u} du$  (E)  $\int_{1}^{4} e^{u} du$

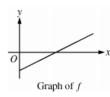
- 13. The function f is defined by  $f(x) = \begin{cases} 2 & \text{for } x < 3 \\ x 1 & \text{for } x \ge 3. \end{cases}$  What is the value of  $\int_{1}^{5} f(x) dx$ ?
  - (A) 2
- (B) 6
- (C) 8
- (D) 10

- 14. If  $f(x) = \sqrt{x^2 4}$  and g(x) = 3x 2, then the derivative of f(g(x)) at x = 3 is

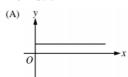
- (A)  $\frac{7}{\sqrt{5}}$  (B)  $\frac{14}{\sqrt{5}}$  (C)  $\frac{18}{\sqrt{5}}$  (D)  $\frac{15}{\sqrt{21}}$  (E)  $\frac{30}{\sqrt{21}}$

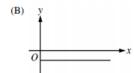


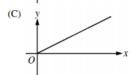
- 15. The graph of a differentiable function f is shown above. If  $h(x) = \int_0^x f(t) dt$ , which of the following is true?
  - (A) h(6) < h'(6) < h''(6)
  - (B) h(6) < h''(6) < h'(6)
  - (C) h'(6) < h(6) < h''(6)
  - (D) h''(6) < h(6) < h'(6)
  - (E) h''(6) < h'(6) < h(6)
- 16. A particle moves along the x-axis with its position at time t given by x(t) = (t-a)(t-b), where a and b are constants and  $a \neq b$ . For which of the following values of t is the particle at rest?
  - (A) t = ab
  - (B)  $t = \frac{a+b}{2}$
  - (C) t = a + b
  - (D) t = 2(a+b)
  - (E) t = a and t = b

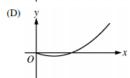


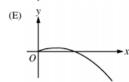
17. The figure above shows the graph of f. If  $f(x) = \int_{2}^{x} g(t) dt$ , which of the following could be the graph of y = g(x)?











- $\lim_{h\to 0} \frac{\ln(4+h) \ln(4)}{h}$  is

  - (A) 0 (B)  $\frac{1}{4}$ 
    - (C) 1
- (D) e
- (E) nonexistent

- 19. The function f is defined by  $f(x) = \frac{x}{x+2}$ . What points (x,y) on the graph of f have the property that the line tangent to f at (x,y) has slope  $\frac{1}{2}$ ?
  - (A) (0,0) only
  - (B)  $\left(\frac{1}{2}, \frac{1}{5}\right)$  only
  - (C) (0,0) and (-4,2)
  - (D) (0,0) and  $\left(4,\frac{2}{3}\right)$
  - (E) There are no such points.
- 20. Let  $f(x) = (2x + 1)^3$  and let g be the inverse function of f. Given that f(0) = 1, what is the value of g'(1)?
  - (A)  $-\frac{2}{27}$  (B)  $\frac{1}{54}$  (C)  $\frac{1}{27}$  (D)  $\frac{1}{6}$  (E) 6

- 21. The line y = 5 is a horizontal asymptote to the graph of which of the following functions?

$$(A) \quad y = \frac{\sin(5x)}{x}$$

(B) 
$$y = 5$$

(C) 
$$y = \frac{1}{x}$$

(D) 
$$y = \frac{5x}{1-x}$$

- (A)  $y = \frac{\sin(5x)}{x}$  (B) y = 5x (C)  $y = \frac{1}{x-5}$  (D)  $y = \frac{5x}{1-x}$  (E)  $y = \frac{20x^2 x}{1+x^2}$
- 22. Let f be the function defined by  $f(x) = \frac{\ln x}{x}$ . What is the absolute maximum value of f?
  - (A) 1
  - (B)  $\frac{1}{e}$
  - (C) 0
  - (D) −e
  - (E) f does not have an absolute maximum value.
- 23. If P(t) is the size of a population at time t, which of the following differential equations describes linear growth in the size of the population?
  - (A)  $\frac{dP}{dt} = 200$
  - (B)  $\frac{dP}{dt} = 200t$
  - (C)  $\frac{dP}{dt} = 100t^2$
  - (D)  $\frac{dP}{dt} = 200P$
  - (E)  $\frac{dP}{dt} = 100P^2$

24. Let $g$ be the function given by	$g(x) = x^2 e^{kx}$ , whe	re k is a constant	. For what value o	f k does g	have a critica
point at $x = \frac{2}{3}$ ?					

- (A) -3 (B)  $-\frac{3}{2}$  (C)  $-\frac{1}{3}$  (D) 0 (E) There is no such k.
- 25. Which of the following is the solution to the differential equation  $\frac{dy}{dx} = 2\sin x$  with the initial condition  $y(\pi) = 1$ ?
  - (A)  $y = 2\cos x + 3$
  - (B)  $y = 2\cos x 1$
  - (C)  $y = -2\cos x + 3$
  - (D)  $y = -2\cos x + 1$
  - (E)  $y = -2\cos x 1$
- 26. Let g be a function with first derivative given by  $g'(x) = \int_0^x e^{-t^2} dt$ . Which of the following must be true on the interval 0 < x < 2?
  - (A) g is increasing, and the graph of g is concave up.
  - (B) g is increasing, and the graph of g is concave down.
  - (C) g is decreasing, and the graph of g is concave up.
  - (D) g is decreasing, and the graph of g is concave down.
  - (E) g is decreasing, and the graph of g has a point of inflection on 0 < x < 2.
- 27. If  $(x + 2y) \cdot \frac{dy}{dx} = 2x y$ , what is the value of  $\frac{d^2y}{dx^2}$  at the point (3, 0)?

- (A)  $-\frac{10}{3}$  (B) 0 (C) 2 (D)  $\frac{10}{3}$  (E) Undefined
- 28. For  $t \ge 0$ , the position of a particle moving along the x-axis is given by  $x(t) = \sin t \cos t$ . What is the acceleration of the particle at the point where the velocity is first equal to 0?
  - $(A) -\sqrt{2}$
- (B) −1
- (C) 0
- (D) 1
- (E) √2